

## UNIVERSITY OF PERADENIYA

## දුරස්ථ හා අඛණ්ඩ අධාාපන කේන්දුය தொடர் தொலைக் கல்வி நிலையம் CENTRE FOR DISTANCE AND CONTINUING EDUCATION



පළමු වසර ශාස්තුවේදී උපාධි පරීකෲණය (බාහිර-නව නිර්දේශය) දෙසැමබර් 2018 முதலாம் வருட (100 LEVEL) கலைத்தேர்வுப் பரீட்சை (வெளிவாரி - புதிய பாடத்திட்டம்) மார்கழி - 2018

1st YEAR (100 LEVEL) EXAMINATION IN BACHELOR OF ARTS (EXTERNAL - NEW SYLLABUS) DECEMBER 2018

## **FNDE 102 - Basic Mathematics**

## **Instructions:**

- 1. There are eight (08) questions in this paper. Answer any five (05) questions.
- 2. Time: Three (03) hours.
- 3. Calculators are not allowed.
- 4. Total marks: 100
- 1. (a) Simplify the following.

(i). 
$$\frac{x^2y}{2xy^2}$$
 (ii)  $\frac{(\sqrt{2x})^4}{(4x^2y^2)^3}$  (iii)  $\frac{(5a^3)^4}{25a^2}$  (iv)  $\sqrt{49x^6y^4}$ 

(2.5 marks each)

- (b) Factorize the following polynomials.
  - (i).  $x^2 36y^2$

(iv)  $3xy - 9y^2$ 

- (ii).  $16x^3 54$
- (v)  $16x^2 24x 160$
- (iii).  $3x^2 + 10x + 8$

(02 marks each)

- 2. (a) Solve the following.
  - (i). 5x + 9 = 3x 7

(ii). 
$$\frac{3x+2}{2} = \frac{x-1}{4}$$

(05 marks each)

- (b) Draw the following inequalities in a number line.
  - (i).  $-2 \le x \le 2$

(ii) 
$$x \le 0$$
 or  $x \ge 3$ 

(04 marks)

- (c) Solve the following inequalities and graph the solutions.
  - (i).  $5-2x \ge x+4$

(i). 
$$5(1-3x) \ge 8$$

(03 marks each)

3. (a) Solve the following simultaneous equations. Verify your solution by drawing the equations in a graph.

$$x + 2y = 4$$

$$3x - y = 5$$

(10 marks)

(b) A child bought two types of toffees. Price of one type of toffees is Rs. 2 each and the other type of toffees cost Rs. 3 each. If the child has bought 15 toffees and the total cost of toffees is Rs. 38, how many toffees from each of the types were purchased?

(10 marks)

- 4. Consider the function  $y = x^2 + 2x 3$  where for  $-3 \le x \le 3$ 
  - (a) Verify whether the graph of the function takes a U-shape or an inverted U-shape.

(04 marks)

(b) Find the stationary points of the function if any.

(06 marks)

(c) Draw the graph of the function.

(10 marks)

5. Solve the following limits.

(a) 
$$\lim_{x \to 2} \frac{2x^2 - 8}{x - 2}$$

(c)  $\lim_{x \to 0} \frac{(x+2)^2 - 4}{x}$ 

(b) 
$$\lim_{x \to \infty} \frac{2x^2 + 3x + 1}{x^2 + 4x + 5}$$

(d)  $\lim_{x \to 1} \frac{(x^2 + 4x + 3)}{(x+3)}$ 

(05 marks each)

6. Differentiate the following functions.

(a) 
$$y = 2x^5 + 7x^{1/2} + \frac{1}{x^3}$$

(d)  $y = x^3 e^{3x}$ 

(b) 
$$y = (2x^2 + 1)(4x + 3)$$

(e)  $y = \ln(2x)$ 

(c) 
$$y = \frac{x^2 + 5x - 3}{3x^2}$$

(04 marks each)

7. Integrate the following functions.

(a) 
$$\int (x^4 - 6x^{1/2}) dx$$

(b) 
$$\int 2e^{4x}dx$$

(c) 
$$\int (1-2x)^3 dx$$

(d) 
$$\int \frac{13x}{7x^2 + 5} dx$$

(e) Use the substitution 
$$u = x^2 - 4x + 5$$
 to evaluate  $\int \frac{x-2}{x^2 - 4x + 5} dx$  (04 marks each)

- 8. (a) In a class of 43 students, 12 play football and 7 play rugby and 5 play both football and rugby. A student is chosen at randomly. Find the probability that the student,
  - (i). Plays football.
  - (ii). Plays both.
  - (iii). Plays football or rugby.
  - (iv). Plays neither of these sports.

(10 marks)

- (b) A box contains 4 blue and 3 yellow buttons of the same size. Two buttons are randomly selected from the box without replacement. Find the probability that
  - (i). Both are yellow.
  - (ii). The first is yellow and the second is blue.

(10 marks)